

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATICS			0580/43
Paper 4 (Extended)		October/N	lovember 2016
		2 hou	urs 30 minutes
Candidates answer on	the Question Paper.		
Additional Materials:	Electronic calculator	Geometrical instruments	

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Tracing paper (optional)

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.





(a)	A jigsaw puzzle has edge pieces and inside pieces. The ratio edge pieces: inside pieces = 3:22.							
	(i)	There are 924 inside pieces.						
		Calculate the total number of pieces in the puzzle.						
			[2]					
	(ii)	Find the percentage of the total number of pieces that are edge pieces.						
			% [1]					
	(iii)	Anjum and Betty spent a total of 9 hours completing the puzzle. The ratio Anjum's time: Betty's time = 7:5.						
		Work out how much time Anjum spent on the puzzle.						
			hours [2]					
(b)		e price of the puzzle was \$15.99 in a sale. is was 35% less than the original price.	hours [2]					
		lculate the original price of the puzzle.						
		\$	[3]					

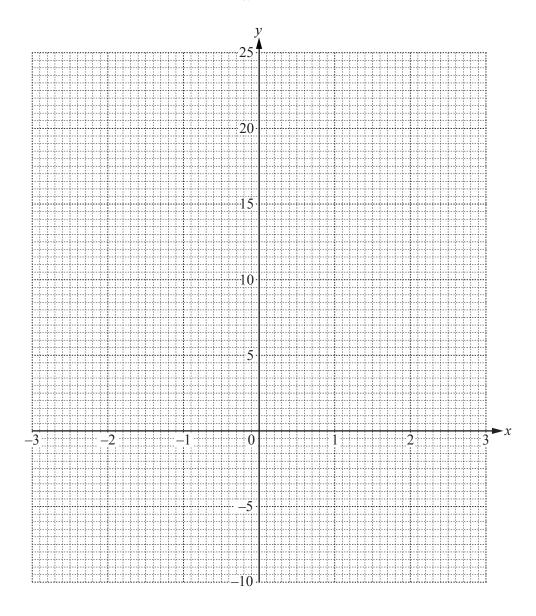
(c)	Betty takes a photograph of the completed puzzle. The photograph and the completed puzzle are mathematically similar.				
	The The	e area of the photograph is 875 cm ² and the area of the puzzle is length of the photograph is 35 cm.	$2835\mathrm{cm}^2$.		
	Wor	rk out the length of the puzzle.			
			cm [3]		
(d)	(i)	The area of another puzzle is 6610 cm ² .			
		Change 6610 cm ² into m ² .			
			m ² [1]		
	(ii)	The cost price of this puzzle is \$12.50. The selling price is \$18.50.			
		Calculate the percentage profit.			
			% [3]		

2 (a) Complete the table for $y = 3x + \frac{2}{x^2} + 1$, $x \ne 0$.

х	-3	-2	-1	-0.5	-0.3	0.3	0.5	1	2	3
У	-7.8		0	7.5	22.3	24.1		6	7.5	10.2

[2]

(b) On the grid, draw the graph of $y = 3x + \frac{2}{x^2} + 1$ for $-3 \le x \le -0.3$ and $0.3 \le x \le 3$.



[5]

(c) Write down the value of the largest integer, k, so that the equation $3x + \frac{2}{x^2} + 1 = k$ has exactly one solution.

$$k = \dots$$

(d) (i) By drawing a suitable straight line on the grid, solve $3x + \frac{2}{x^2} + 1$

$$x =$$
 or $x =$ [4]

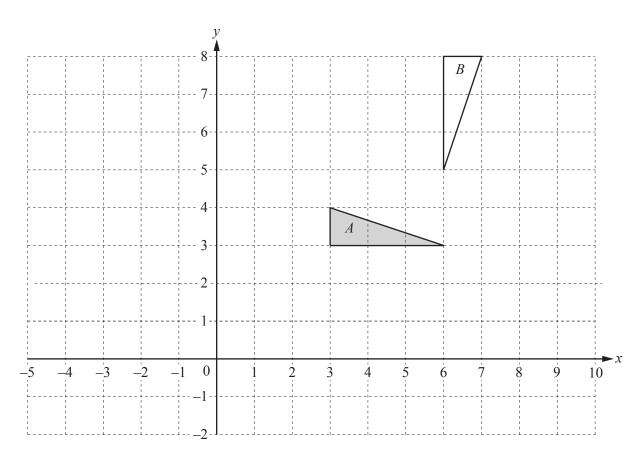
(ii) The equation $3x + \frac{2}{x^2} + 1 = 15 - 3x$ can be written in the form $ax^3 + bx^2 + cx + 2 = 0$, where a, b and c are integers.

Find a, b and c.

a =				

$$c = \dots [3]$$

3	(a)	Solve.	8x - 5 = 22 - 4x	v	
	(b)	Solve.	$6x \geqslant 2x + 14$		<i>x</i> =[2]
	(c)	Factorise	$x^{2} - 4x - 21$		[2]
	(d)	Expand t	he brackets and simplify.	(3x - 2y)(4x + 3y)	[2]
					[3]

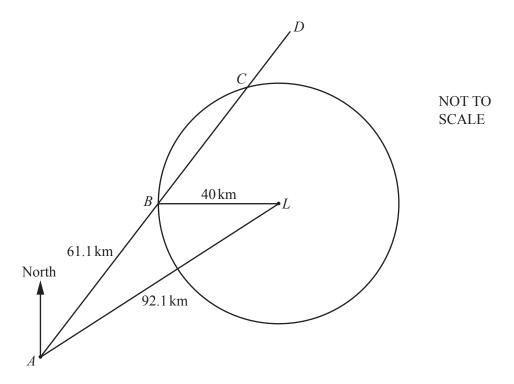


- (a) Draw the image when triangle A is reflected in the line x = 1. [2]
- **(b)** Draw the image when triangle *A* is translated by the vector $\binom{-2}{3}$.
- (c) Draw the image when triangle A is enlarged by scale factor 2 with centre (4, 5). [2]
- (d) Describe fully the **single** transformation that maps triangle A onto triangle B.

8 5 Sandra has a fair eight-sided spinner. The numbers on the spinner are 3, 4, 4, 4, 5, 5, 6 and 8. Sandra spins the spinner twice and records each number it lands on. Find the probability that (a) both numbers are 8,[2] **(b)** the two numbers are not both 8,[1] (c) one number is odd and one number is even,

.....[2]

(d)	the total of the two numbers is at least 13,	
		[3]
(e)	the second number is bigger than the first number.	
		[3]



The diagram shows the position of a port, A, and a lighthouse, L.

The circle, centre L and radius $40\,\mathrm{km}$, shows the region where the light from the lighthouse can be seen.

The straight line, ABCD, represents the course taken by a ship after leaving the port.

When the ship reaches position *B* it is due west of the lighthouse.

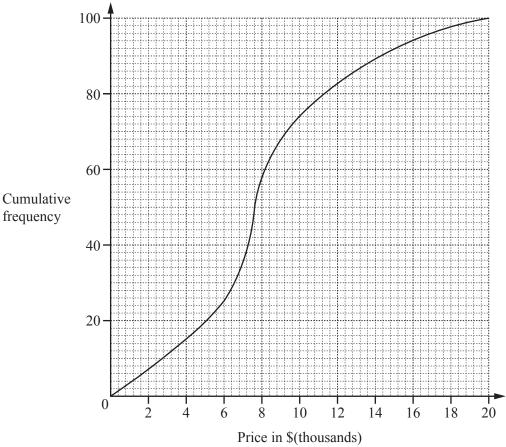
$$AL = 92.1 \,\mathrm{km}$$
, $AB = 61.1 \,\mathrm{km}$ and $BL = 40 \,\mathrm{km}$.

(a) Use the cosine rule to show that angle $ABL = 130.1^{\circ}$, correct to 1 decimal place.

[4]

(b)	Calculate the bearing of the lighthouse, L , from the port, A .
	[4]
(c)	The ship sails at a speed of 28 km/h.
	Calculate the length of time for which the light from the lighthouse can be seen from the ship. Give your answer correct to the nearest minute.
	h min [5]





The cumulative frequency diagram shows information about the prices of 100 cars on Website A. Use the information to complete this table.

Lower quartile	Median	Upper quartile	Inter-quartile range
\$	\$7600	\$	\$

[2]

(ii) This table shows information about the prices of cars on Website B.

Lower quartile	Median	Upper quartile	Inter-quartile range
\$7600	\$10800	\$13 600	\$6000

Here are two statements comparing the distributions of the prices of cars on Website A and Website B.

For each statement write True or False.

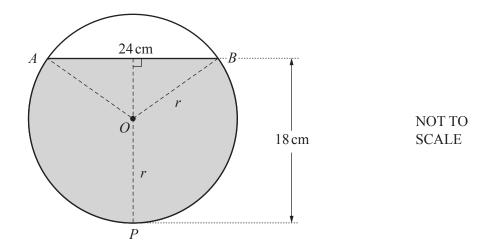
Give a reason for each answer, stating clearly which statistic you use to make your decision.

(a) The prices of cars on Website A are lower than the prices of cars on Website B.

b	because	
		F13

		13		
	(b)	A greater percentage of cars have a pri Website B.	ce more than \$136	000 on Website A compared to
		because		
				[1
(b)	The table	shows the prices of cars on Website B.		
		Price (\$ <i>P</i>)	Number of cars	
		$0 < P \leqslant 6000$	9	
		$6000 < P \le 8000$	29	
		$8000 < P \le 10000$	20	
		$10000 < P \leqslant 12000$	14	
		$12000 < P \le 14000$	21	
		$14000 < P \leqslant 22000$	27	
	Calculate	an estimate of the mean price of the 12	o cars.	
			\$	[4
(c)	Bryan pa	e of a car is \$8760. ys a deposit of 25% of this price and the months, he will have paid a total of \$99		y payments.
	Calculate	the cost of one monthly payment.		

\$.....[3]



The diagram shows the cross section of a cylinder, centre O, radius r, lying on its side. The cylinder contains water to a depth of $18 \, \mathrm{cm}$.

The width, AB, of the surface of the water is 24 cm.

(a) Use an algebraic method to show that r = 13 cm.

[4]

(b) Show that angle $AOB = 134.8^{\circ}$, correct to 1 decimal place.

[2]

(c) (i) Calculate the area of the major sector *OAPB*.

.....cm² [3]

	(ii)	Calculate the area of the shaded segment <i>APB</i> .			
					cm ² [3]
	(iii)	The length of the cylinder is 40 cm.			
		Calculate the volume of water in the cylinder.			
					cm ³ [1]
(d)	The In th	e cylinder is turned so that it stands on one of its circular enhis position, the depth of the water is h .	nds.		
	Find	d <i>h</i> .			
					NOT TO
			h		SCALE
			*		
			<i>l</i> a –	_	om [2]
			rı -		cm [2

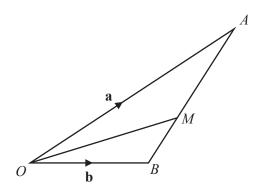
Λ	(-)	(3)	(-2))
9	(a)	$\mathbf{m} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$	$\mathbf{n} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$	/

(i) Work out 2m - 3n.

(ii) Calculate $|2\mathbf{m} - 3\mathbf{n}|$.

.....[2]

(b) (i)



NOT TO SCALE

In the diagram, O is the origin, $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$. The point M lies on AB such that AM : MB = 3 : 2.

Find, in terms of **a** and **b**, in its simplest form

(a) \overrightarrow{AB} ,

$$\overrightarrow{AB} = \dots [1]$$

(b) \overrightarrow{AM} ,

$$\overrightarrow{AM} = \dots [1]$$

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(c) the position vector of M.

		[2]
(ii)	OM is extended to the point C . The position vector of C is $\mathbf{a} + k\mathbf{b}$. Find the value of k .	
		k =[1]

10 (a) Complete the table for the four sequences A, B, C and D.

	Sequence				Next term	<i>n</i> th term
A	2	5	8	11		
В	20	14	8	2		
С	1	4	9	16		
D	0	2	6	12		

[10]

- **(b)** The sum of the first *n* terms of a sequence is $\frac{n(3n+1)}{2}$.
 - (i) When the sum of the first *n* terms is 155, show that $3n^2 + n 310 = 0$.

[2]

(ii) Solve $3n^2 + n - 310 = 0$.

(iii) Complete the statement.

The sum of the first terms of this sequence is 155. [1]

11 Solve.
$$\frac{2}{x+3} + \frac{1}{12} = \frac{3}{2x-1}$$

$$x =$$
..... or $x =$ [7]

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